

INTRODUCTION TO BIOSTATISTICS

How to read the standard normal table

(Table A.3 of Principles of Biostatistics, Pagano, M. and Gauvreau, K.)

When reading a normal table, we take advantage of the following features of the normal distribution:

- The **symmetry** of the standard normal curve around zero (its mean). Thus, $P(Z \geq z) = P(Z \leq -z)$, where $z \geq 0$.
- The fact that (as in any distribution) the area under the curve is equal to 1. Thus, $\{Z \geq z\}$ and $\{Z \leq z\}$ are two complementary events, $P(Z \geq z) = 1 - P(Z \leq z)$.

We are usually faced with two problems:

1. Given a number $z \geq 0$ ¹ (say) find p such that the following is true:

- 1.1. $P(Z \geq z) = p$ Read p directly from standard normal table².
- 1.2 $P(Z \leq -z) = p$ Read $p_1 = P(Z \geq z)$ from the normal table
 $p = p_1$ (by the symmetry of the normal distribution)
- 1.3 $P(Z \leq z) = p$ Read $p_1 = P(Z \geq z)$ from the normal table: $p = 1 - p_1$.
Notice that $\{Z \geq z\}$ and $\{Z \leq z\}$ are complementary events
- 1.4 $P(Z \geq -z) = p$ Read $p_1 = P(Z \geq z)$ from the normal table: $p = 1 - p_1$.

Now assume that $z_1 \leq z_2$:

- 1.5 $P(z_1 \leq Z \leq z_2) = p$ Calculate $p_1 = P(Z \geq z_1)$ (if $z_1 \geq 0$ refer to 1.1, if $z_1 < 0$ refer to 1.4) and $p_2 = P(Z \geq z_2)$ (if $z_2 \geq 0$ refer to 1.1, if $z_2 < 0$ refer to 1.4); then $p = p_1 - p_2$

Special case: $z > 0$

- $P(-z \leq Z \leq z)$ Read $p_1 = P(Z \geq z)$ from the normal table $p = 1 - 2p_1$.
Notice that this is the **central** part of the distribution.

2. Given a probability p find z such that the following is true:

- 2.1 $P(Z \geq z) = p$
If $p \leq 0.5$ Then $z \geq 0$: Look up p in table. z is the closest number³.
If $p \geq 0.5$ Then $z \leq 0$: Look up $p_1 = 1 - p$ in the table. Locate the closest number. z is its negative.
- 2.2 $P(Z \leq z) = p$
If $p \leq 0.5$ Then $z \leq 0$: Look up p in table. Locate the closest number.
 z is its negative.
If $p \geq 0.5$ Then $z \geq 0$: Look up $p_1 = 1 - p$ in the table.
 z is the closest number.
- 2.3 $P(-z \leq Z \leq z) = p$ Look up $p_1 = (1 - p)/2$ in the table. z is the closest number.
 $-z$ is its negative.

¹Recall that capital Z is the (normally distributed) random variable, while z is the values it assumes

²The p corresponding to z is read by going “down” in the table as many lines as it’s necessary to approach z as closely as possible (without going over), and then going “across” on the same line, as many columns as it’s necessary to approach z as closely as possible (without going over).

³The “closest number” z corresponding to a given p is found by adding the number in the left margin of the *line* where p is located in the table, to the number at the top margin of the *column* where p is located in the table.